

# 4(4): Resonance Condition for Gravitational Potential

The ECE wave equation is:

$$\nabla^2 \Phi = R \Phi \quad - (1)$$

Let  $\Phi$  is the gravitational potential and  $R$  the scalar curvature. The solution of Eq. (1) is:

$$\Phi = \Phi_0 \exp(i(\omega t - \underline{\kappa} \cdot \underline{r})) \quad - (2)$$

where:

$$\frac{\omega^2}{c^2} - \kappa^2 = R \quad - (3)$$

For gravitostatics it is assumed that:

$$\Phi = \Phi_0 \exp(-i \underline{\kappa}_0 \cdot \underline{r}) \quad - (4)$$

and

$$(\nabla^2 + R) \Phi = 0 \quad - (5)$$

where

$$R = \kappa_0^2 \quad - (6)$$

A small driving force of electromagnetic origin is applied to the gravitational system consisting of a mass  $m$  attracted by a mass  $M$ . Therefore Eq. (5) becomes the Euler Bernoulli equation:

$$(\nabla^2 + R) \Phi = A \cos \underline{\kappa} \cdot \underline{r} \quad - (7)$$

In one dimension:

$$\left( \frac{\partial^2}{\partial z^2} + R \right) \Phi = A \cos \kappa_z z \quad - (8)$$

The electromagnetic driving force is applied along the  $z$  axis.

The solution of Eq. (8) is:

$$\underline{\Phi} = \frac{A \cos \underline{k}_z z}{\underline{k}_0^2 - \underline{k}_z^2} \quad - (9)$$

and counter gravitation occurs under the condition:

$$\underline{k}_0 = \underline{k}_z \quad - (10)$$

when

$$\underline{\Phi} \rightarrow \infty \quad - (11)$$

In ECE2:

$$\underline{g} = -\underline{\nabla} \underline{\Phi} - \frac{\partial \underline{Q}}{\partial t} \quad - (12)$$

and

$$\underline{\nabla} \cdot \underline{g} = 4\pi G \rho_m \quad - (13)$$

where  $\underline{Q}$  is the gravitational vector potential. This does not exist in the standard model of physics. Here  $G$  is Newton's constant and  $\rho_m$  is the source mass density.

So

$$-\underline{\nabla}^2 \underline{\Phi} - \underline{\nabla} \cdot \frac{\partial \underline{Q}}{\partial t} = 4\pi G \rho_m \quad - (14)$$

If it is assumed that:  $\underline{Q} = 0 \quad - (15)$

then:

$$\underline{\nabla}^2 \underline{\Phi} = -4\pi G \rho_m \quad - (16)$$

From eqs. (7) and (16):

$$-4\pi G \rho_m + \underline{k}_0^2 \underline{\Phi} = A \cos \underline{k} \cdot \underline{r} \quad - (17)$$

In one dimension:

$$-4\pi G\rho_m + \kappa_0^2 \Phi = A \cos \kappa_z z - (18)$$

in eqs. (9) and (18):

$$-\cancel{4\pi} G\rho_m + \kappa_0^2 A \cos \kappa_z z = A \cos \kappa_z z - (19)$$

$$\therefore \kappa_0^2 A \cos \kappa_z z = \frac{\kappa_0^2 - \kappa_z^2}{\kappa_0^2 - \kappa_z^2} (A \cos \kappa_z z + \cancel{4\pi} G\rho_m) - (20)$$

From eqs. (10) and (20) the resonance condition is

$$\cos \kappa_z z = 0 - (21)$$

i.e.

$$\boxed{\kappa_z z = \frac{\pi}{2}} - (22)$$

Finally assume that:

$$\kappa_z = \frac{\omega}{c} - (23)$$

then:

$$\boxed{\omega z = \frac{\pi}{2} c} - (24)$$

If  $z$  is as before then: - (25)

$$\omega = 4.709 \times 10^8 \text{ rad/sec}$$

This result seems to be too simple, because mass held as before above the surface of the earth is not elevated by radiating it by  $c/n$  radiation.

The origin of the problem is that  $\Phi$  has been

assumed to be a wave in eq. (1). Hence it has been assumed that there exist gravitational waves. In order for such waves to exist the gravitational vector potential  $\underline{Q}$  has to be non-zero, and the gravitational field must exist. Additionally, in analogy with the Maxwell displacement current, gravitational waves need the existence of the "Maxwell displacement current" of  $E(E_2)$ , i.e.  $\underline{\partial \underline{Q}} / \partial t$ .

So the two relevant equations are:

$$(\nabla^2 + R) \underline{\Phi} = A \cos \underline{\kappa} \cdot \underline{r} \quad - (26)$$

and

$$\nabla^2 \underline{\Phi} + \underline{\nabla} \cdot \frac{\partial \underline{Q}}{\partial t} = -4\pi G \rho_m \quad - (27)$$

Hence:

$$R \underline{\Phi} - \underline{\nabla} \cdot \frac{\partial \underline{Q}}{\partial t} - 4\pi G \rho_m = A \cos \underline{\kappa} \cdot \underline{r} \quad - (28)$$

In the direction:

$$\frac{\kappa_0^2 A \kappa_z Z}{\kappa_0^2 - \kappa_z^2} - 4\pi G \rho_m - \underline{\nabla} \cdot \frac{\partial \underline{Q}}{\partial t} = A \cos \kappa_z Z \quad - (29)$$

$$\kappa_0^2 A \kappa_z Z = (\kappa_0^2 - \kappa_z^2) \left( A \cos \kappa_z Z + \underline{\nabla} \cdot \frac{\partial \underline{Q}}{\partial t} + 4\pi G \rho_m \right)$$

However, it is clearer to use:

$$\nabla^2 \underline{\Phi} = -\kappa_z^2 \underline{\Phi} \quad - (30)$$

in eq. (27), so:

$$- \kappa_z^2 \underline{\Phi} + \underline{\nabla} \cdot \frac{\partial \underline{Q}}{\partial t} = - \frac{4\pi \epsilon_0}{m} - (31)$$

where

$$\underline{\Phi} = \frac{A \cos \kappa_z z}{\kappa_0^2 - \kappa_z^2} - (32)$$

$$\text{so } \frac{A \kappa_z^2 \cos \kappa_z z}{\kappa_0^2 - \kappa_z^2} = \underline{\nabla} \cdot \frac{\partial \underline{Q}}{\partial t} + \frac{4\pi \epsilon_0}{m} - (33)$$

so at resonance:

$$\boxed{\underline{\nabla} \cdot \frac{\partial \underline{Q}}{\partial t} \rightarrow \infty} - (34)$$

when:

$$\kappa_0 = \kappa_z - (35)$$

and

$$\underline{\Phi} \rightarrow \infty. - (36)$$

In order for this method to work the electromagnetic frequency  $\omega_z$  must be tuned to a characteristic frequency  $\omega_0 = \kappa_0 c$ .

If it is assumed that  $\underline{g}$  is not a wave,

then

$$\underline{g} = - \underline{\nabla} \underline{\Phi} - (37)$$

More generally,

$$\underline{g} = - \underline{\nabla} \underline{\Phi} - 2 \underline{\Phi} \underline{\omega} + 2 c \omega_0 \underline{Q} - \frac{\partial \underline{Q}}{\partial t} - (38)$$